Cross-Reaction and categorical interpretation

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Introduction

Cross-Reaction 1000 pages soon

- Description of the category of models and a glide path from Kripke to HOTT
- Definition of the category of models
- Definition of the category of models for Classical Propositional Logic (the category of Boolean algebras and homomorphisms between them) and for Intuitionistic Propositional Logic (the category of Heyting algebras and homomorphisms between them)

Building models for Classical Propositional Logic from the algebraic viewpoint: **Tarski's theorem** (Lindenbaum-Tarski construction). Soundness and completeness. Compactness. Decidability. Lindenbaum algebras. Stone's representation theorem for Boolean algebras. Duality between Boolean algebras and Stone spaces. Stone's theorem for finite Boolean algebras. Tarski's theorem for finite Boolean algebras. Tarski's theorem for finite Boolean algebras as a categorical equivalence. Tarski's theorem for finite Boolean algebras as a categorical duality. Tarski's theorem for finite Boolean algebras as a contravariant functor. Tarski's theorem for finite Boolean algebras as a contravariant equivalence. Tarski's theorem for finite Boolean algebras as a contravariant duality.

Building models for Intuitionistic Propositional Logic from the algebraic viewpoint: Heyting algebras. Lindenbaum algebras. Soundness and completeness. Compactness. Decidability. Duality between Heyting algebras and Esakia spaces. Esakia's theorem for finite Heyting algebras. Esakia's theorem for finite Heyting algebras as a categorical equivalence. Esakia's theorem for finite Heyting algebras as a categorical duality. Esakia's theorem for finite Heyting algebras as a contravariant functor. Esakia's theorem for finite Heyting algebras as a contravariant equivalence. Esakia's theorem for finite Heyting algebras as a contravariant duality.

Tarski's topological semantics for Intuitionistic Propositional Logic. Soundness and completeness. Compactness. Decidability. Duality between Heyting algebras and Tarski spaces. Tarski's theorem for finite Heyting algebras. Tarski's theorem for finite Heyting algebras as a categorical equivalence. Tarski's theorem for finite Heyting algebras as a categorical duality. Tarski's theorem for finite Heyting algebras as a contravariant functor. Tarski's theorem for finite Heyting algebras as a contravariant equivalence. Tarski's theorem for finite Heyting algebras as a contravariant duality.

Kripke's semantics for Intuitionistic Propositional Logic. Soundness and completeness. Compactness. Decidability. Duality between Heyting algebras and Kripke frames. Kripke's theorem for finite Heyting algebras. Kripke's theorem for finite Heyting algebras as a categorical equivalence. Kripke's theorem for finite Heyting algebras as a categorical duality. Kripke's theorem for finite Heyting algebras as a contravariant functor. Kripke's theorem for finite Heyting algebras as a contravariant equivalence. Kripke's theorem for finite Heyting algebras as a contravariant duality.

Kripke's semantics for Classical Propositional Logic. Soundness and completeness. Compactness. Decidability. Duality between Boolean algebras and Kripke frames. Kripke's theorem for finite Boolean algebras. Kripke's theorem for finite Boolean algebras as a categorical equivalence. Kripke's theorem for finite Boolean algebras as a categorical duality. Kripke's theorem for finite Boolean algebras as a contravariant functor. Kripke's theorem for finite Boolean algebras as a contravariant equivalence. Kripke's theorem for finite Boolean algebras as a contravariant duality.

Kripke's semantics for Modal Propositional Logic. Soundness and completeness. Compactness. Decidability. Duality between Modal algebras and Kripke frames. Kripke's theorem for finite Modal algebras. Kripke's theorem for finite Modal algebras as a categorical equivalence. Kripke's theorem for finite Modal algebras as a categorical duality. Kripke's theorem for finite Modal algebras as a contravariant functor. Kripke's theorem for finite Modal algebras as a contravariant equivalence. Kripke's theorem for finite Modal algebras as a contravariant duality.

Kripke's semantics for Intuitionistic Modal Propositional Logic. Soundness and completeness. Compactness. Decidability. Duality between Modal algebras and Kripke frames. Kripke's theorem for finite Modal algebras. Kripke's theorem for finite Modal algebras as a categorical equivalence. Kripke's theorem for finite Modal algebras as a categorical duality. Kripke's theorem for finite Modal algebras as a contravariant functor. Kripke's theorem for finite Modal algebras as a contravariant equivalence. Kripke's theorem for finite Modal algebras as a contravariant duality.

Kripke's semantics for Classical